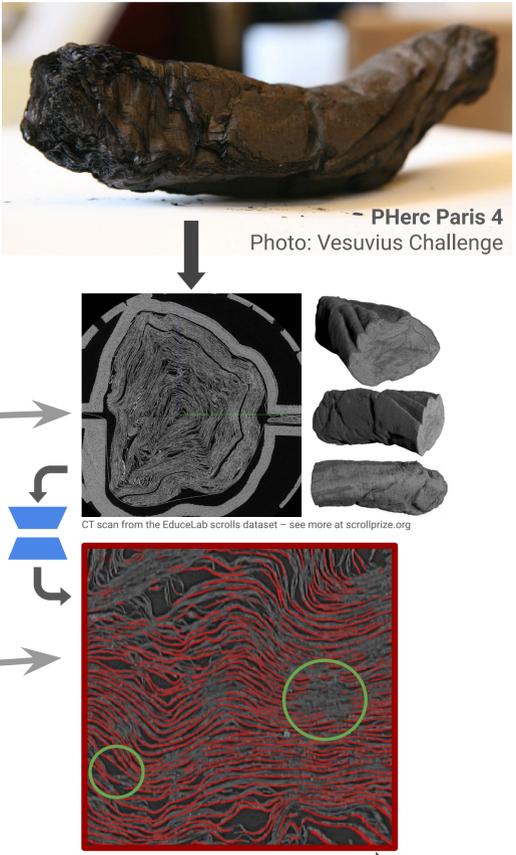


Virtually Unrolling the Herculaneum Papyri by Diffeomorphic Spiral Fitting

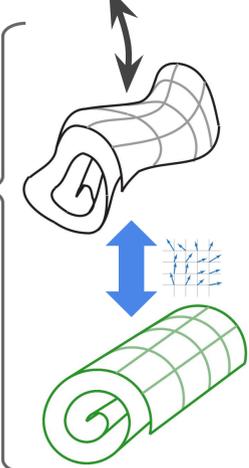
Paul Henderson



- **AD79**: papyrus scrolls charred & buried by Mount Vesuvius
- excavated starting c1752
- many are **impossible** to unroll physically
- solution: μ CT scans + **virtual unrolling**
 - seek a 2D mesh representation of where the original papyrus surface passes in 3D
- **but**: CTs look like *this* 🤔
 - very dense
 - very distorted
 - some wraps broken / missing
- neural networks can *kinda* localise the sheet – but many gaps & false joins
- cannot easily 'read off' a 2D surface mesh



- ### Idea
- the physical scroll is a rectangular sheet, rolled up, then badly distorted following the eruption
 - our aim: **invert** this process, *i.e.* find a 'good' **rolled sheet + deformation** that explains the observed **scan data**
 - the deformation is a **diffeomorphism** that distorts an **ideal scroll** into the shape in the scans
 - very different to existing bottom-up methods!



Model

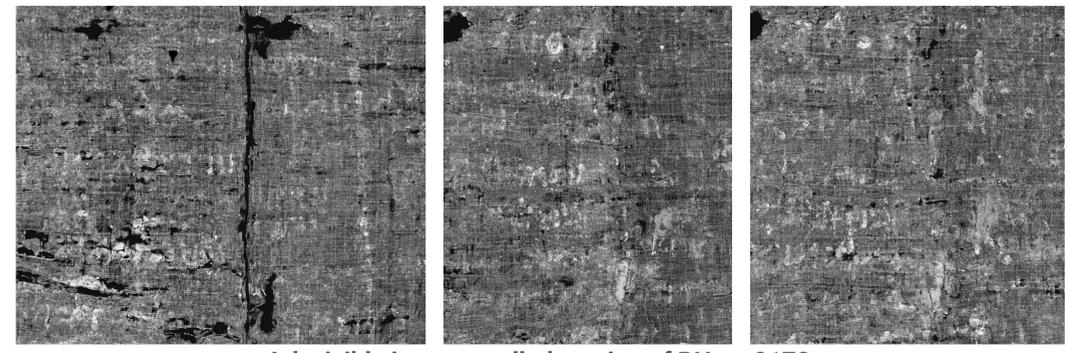
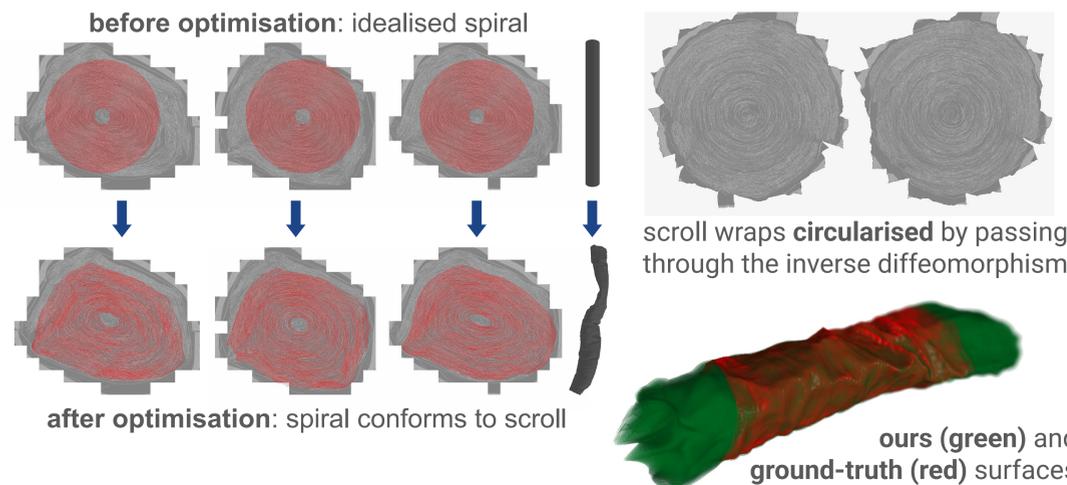
- ideal scroll: extruded archimedean spiral $s(\theta, z; \omega) = \begin{pmatrix} \frac{\theta}{\omega} \cos \theta \\ -\frac{\theta}{\omega} \sin \theta \\ z \end{pmatrix}$
 - free parameter: winding rate ω
- deformation: three **diffeomorphic** stages
 - z-dependent global xy-scale
 - integrated constant velocity field $\begin{cases} \frac{d}{dt} \phi^{(t)}(\mathbf{x}) = \mathbf{u}(\phi^{(t)}(\mathbf{x})) \\ T_{\text{flow}}(\mathbf{x}) = \phi^{(1)}(\mathbf{x}) \\ \phi^{(0)}(\mathbf{x}) = \mathbf{x} \end{cases}$
 - local scaling of winding gaps

Fitting

- **targets**: use pre-trained nnUNet to extract (imperfect) **surfaces, papyrus fibers, and normals**
-
- optimise **winding density & diffeomorphism** jointly to match these
 - **losses**:
 - (deformed) spiral normals match predictions
 - points on the same predicted surface (connected component) lie on the same deformed spiral winding
 - average spacing of deformed spiral windings matches that of predicted surfaces
 - each predicted surface/fiber is near one spiral winding

Results

- validated on two Herculaneum papyri
- quantitative results better *ThaumatoAnakalyptor*, the only other fully-automated approach that can tackle large portions of these scrolls



Ink visible in our unrolled version of PHERC 0172



Ink detected in our unrolled version of PHERC Paris 4